# Foundations of Modern Macroeconomics Second Edition

Chapter 9: Macroeconomics policy, credibility, and politics

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#### Outline

- 1 Dynamic inconsistency and inflation
- 2 Voting and delegation
- Taxation and consistency

#### Aims of this lecture

- What do we mean by *dynamic inconsistency*?
- How can reputation effects help in solving the problem?
- Why do we appoint conservative central bankers?
- Why does taxing capital lead to dynamic inconsistency?

## Dynamic inconsistency (1)

- Monetary policy: policy maker exploits the Lucas supply curve.
- The Lucas supply curve is:

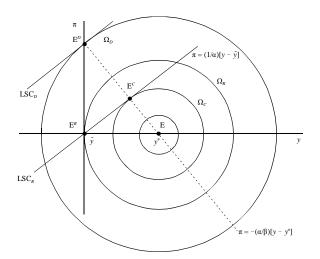
$$y = \bar{y} + \alpha \left[\pi - \pi^e\right] + \varepsilon, \quad \alpha > 0$$

- $y(\bar{y})$  is the logarithm of (full employment) output.
- $\pi$  is actual inflation.
- $\pi^e$  is expected inflation.
- $\varepsilon$  is a stochastic supply shock [observable to policy maker but not to public].
- LSC can be inverted:

$$\pi = \pi^e + (1/\alpha) \left[ y - \bar{y} - \varepsilon \right]$$

In terms of Figure 9.1 the LSC curves are upward sloping lines with a vertical intercept at the level of  $\pi^e$ .

## Figure 9.1: Consistent and optimal monetary policy



## Dynamic inconsistency (2)

 The objective function of the policy maker [social welfare function]:

$$\Omega \equiv \frac{1}{2} [y - y^*]^2 + \frac{\beta}{2} \pi^2, \ \beta > 0$$

- $y^*$  is desired output target of the policy maker.
- $y^* > \bar{y}$ ; policy maker deems  $\bar{y}$  to be too low [overly ambitious?  $\bar{y}$  distorted?].
- $\beta$  measures the relative inflation-aversion of the policy maker [ high  $\beta$  is a right-winger].
- Policy maker chooses  $\pi$  (by monetary policy) and thus y to minimize  $\Omega$  subject to the Lucas supply curve.
- The Lagrangian is:

$$\min_{\{\pi,y\}} \mathcal{L} \equiv \frac{1}{2} \left[ y - y^* \right]^2 + \frac{\beta}{2} \pi^2 + \lambda \left[ y - \bar{y} - \alpha (\pi - \pi^e) - \varepsilon \right]$$

## Dynamic inconsistency (3)

First-order conditions:

$$\frac{\partial \mathcal{L}}{\partial y} = (y - y^*) + \lambda = 0$$
$$\frac{\partial \mathcal{L}}{\partial \pi} = \beta \pi - \alpha \lambda = 0$$

where  $\lambda$  is the Lagrange multiplier.

• Combining the two FONCs yields the "social expansion path" [combinations of  $\pi$  and y for which  $\Omega$  is minimized]:

$$y - y^* = -(\beta/\alpha)\pi \Leftrightarrow$$

$$\pi = -(\alpha/\beta)[y - y^*]$$
(S1)

In terms of Figure 9.1, the FONC is a downward sloping [dashed] line through  $y^*$ .

## Dynamic inconsistency (4)

• The optimal solution under discretionary policy is computed by combining (S1) with the constraint and solving for the inflation rate,  $\pi_D$ :

$$\pi_D = \frac{\alpha^2 \pi^e + \alpha \left[ y^* - \bar{y} - \varepsilon \right]}{\alpha^2 + \beta} \tag{S2}$$

In terms of Figure 9.1, all points on the line between  $\mathsf{E}^D$  and  $\mathsf{E}$  are solutions for  $\pi_D$  for a particular expected price level  $(\pi^e)$ .

 By invoking the rational expectations hypothesis [REH] we find a unique solution for the inflation rate under discretionary policy.

## Dynamic inconsistency (5)

- Derivation:
  - By REH we have  $\pi^e = E(\pi_D)$ .
  - From (S2) we get:  $E(\pi_D)=\frac{\alpha^2\pi^e+\alpha[y^*-\bar{y}-\overbrace{E(\varepsilon)}]}{\alpha^2+\beta}=\pi^e$

so that we can solve for  $\pi^e$ :

$$\pi^e = \frac{\alpha}{\beta} \left[ y^* - \bar{y} \right] \tag{S3}$$

 Substituting (S3) into (S2) and the LSC we find the actual inflation rate:

$$\pi_D = (\alpha/\beta) [y^* - \bar{y}] - \frac{\alpha}{\alpha^2 + \beta} \varepsilon$$
$$y_D = \bar{y} + \frac{\beta}{\alpha^2 + \beta} \varepsilon$$

In Figure 9.1 this is represented by point  $\mathsf{E}^D$ .

## Dynamic inconsistency (6)

• But the discretionary solution  $(\pi_D, y_D)$  is sub-optimal! If the policy maker commits to a zero-inflation rule  $(\pi_R = 0)$  and households would expect it to stick to the rule [so that  $\pi^e = 0$  also] then output would be:

$$y_R = \bar{y} + \varepsilon$$

In terms of Figure 9.1 the rule-based solution  $(\pi_R, y_R)$  is found in point  $\mathsf{E}^R$ . [Later on we shall use "R" to denote reputation.] Social welfare is higher in  $\mathsf{E}^R$  than in  $\mathsf{E}^D$ .

• But unfortunately the rule-based solution is  $(\pi_R, y_R)$  inconsistent! If the policy maker is able to convince the public that it will follow the rule [so that  $\pi^e = 0$ ] then the policy maker is tempted to produce "surprise inflation" to steer the economy towards  $y^*$ . In terms of Figure 9.1 the "cheating solution" [subscript C] lies at point  $\mathbf{E}^C$ .

## Dynamic inconsistency (7)

We find:

$$\pi_C = \frac{\alpha [y^* - \bar{y} - \varepsilon]}{\alpha^2 + \beta}$$

$$y_C = \frac{\beta}{\alpha^2 + \beta} \bar{y} + \frac{\alpha^2}{\alpha^2 + \beta} y^* + \frac{\beta}{\alpha^2 + \beta} \varepsilon$$

• It follows from the diagram that:

$$\Omega_D > \Omega_R > \Omega_C > 0$$

- Discretion: satisfies REH but is sub-optimal [worst of all cases].
- Rule: optimal and satisfies REH. But is open to temptation and thus not credible.
- Cheating: closest to bliss but inconsistent with REH.

## Reputation as an enforcement mechanism (1)

- Idea presented by Barro & Gordon (1983). Key idea:
  - Monetary policy is like a prisoners' dilemma [PD] game. If we only consider solution consistent with the REH then  $(\pi_R, y_R)$  is preferable over  $(\pi_D, y_D)$  but society nevertheless ends up with the worst case.
  - Repeated interactions may help mitigate the PD problem.
     Barro and Gordon suggest that the reputation of the policy maker may act as an enforcement mechanism which makes the rule-based solution credible
- Model is inherently dynamic [reputation is an asset that can be accumulated or decumulated!].

## Reputation as an enforcement mechanism (2)

• The social welfare function is now:

$$V \equiv \Omega_0 + \frac{\Omega_1}{1+r} + \frac{\Omega_2}{(1+r)^2} + \dots = \sum_{t=0}^{\infty} \frac{\Omega_t}{(1+r)^t}$$

where r is the discount factor [interest rate] and  $\Omega_t$  is:

$$\Omega_t \equiv \frac{1}{2} \left[ y_t - y^* \right]^2 + \frac{\beta}{2} \pi_t^2$$

The Lucas supply is deterministic:

$$y_t = \bar{y} + \alpha \left[ \pi_t - \pi_t^e \right], \quad \alpha > 0$$

 Again we look at three types of solution, discretion [D], rule-based [R], and cheating [C].

## Policy under discretion

 From our previous discussion we see that under discretion we would have:

$$\pi_{D,t} = (\alpha/\beta) \left[ y^* - \bar{y} \right]$$

So that:

$$V^{D} \equiv \frac{1+r}{r}\Omega_{D}$$

$$\Omega_{D} \equiv \frac{1}{2}\frac{\alpha^{2}+\beta}{\beta}\left[\bar{y}-y^{*}\right]^{2}$$

## Policy under a constant-inflation rule

- The policy maker follows the rule  $\pi_t = \pi_R$  [a constant]. The REH implies  $E(\pi_t) = \pi_R$ .
- From our earlier discussion we find that:

$$\Omega_R = \frac{1}{2} \left[ \bar{y} - y^* \right]^2$$

can be generalized [for a non-zero  $\pi_R$ ] to:

$$\Omega_R(\pi_R) = \Omega_R + \frac{\beta}{2}\pi_R^2$$

• The social welfare function under the rule-based solution is:

$$V^{R}(\pi_{R}) \equiv \frac{1+r}{r} \left[ \Omega_{R} + \frac{\beta}{2} \pi_{R}^{2} \right]$$

## Cheating solution

• If the policy maker manages to make the agent expect that the rule will be followed  $[\pi^e = \pi_R]$  then he has the incentive to cheat by exploiting the Lucas supply curve associated with  $\pi^e = \pi_R$ . The result is:

$$\pi_C = \frac{\alpha^2 \pi_R + \alpha [y^* - \bar{y}]}{\alpha^2 + \beta}$$

$$y_C = \frac{\beta}{\alpha^2 + \beta} \bar{y} + \frac{\alpha^2}{\alpha^2 + \beta} y^* - \frac{\alpha \beta}{\alpha^2 + \beta} \pi_R$$

so that the objective function under cheating is:

$$\Omega_C(\pi_R) = \frac{1}{2} \left[ \frac{\beta}{\alpha^2 + \beta} \left[ \bar{y} - y^* \right] - \frac{\alpha \beta}{\alpha^2 + \beta} \pi_R \right]^2 + \frac{\beta}{2} \left[ \frac{\alpha^2}{\alpha^2 + \beta} \pi_R + \frac{\alpha}{\alpha^2 + \beta} \left[ y^* - \bar{y} \right] \right]^2$$

## Reputation (1)

 We now introduce the following reputation mechanism ["tit-for-tat"]:

$$\pi_t^e = \begin{cases} \pi_R & \text{if } \pi_{t-1} = \pi_{t-1}^e \\ \pi_{D,t} & \text{if } \pi_{t-1} \neq \pi_{t-1}^e \end{cases}$$

- If the policy maker did in the last period what the public expected him to do  $(\pi_{t-1} = \pi_{t-1}^e)$  then this policy maker has credibility and the public expects that the rule inflation rate  $(\pi_R)$  will be produced in the present period.
- If the policy maker did not do in the last period what the public expected him to do  $(\pi_{t-1} \neq \pi^e_{t-1})$  then this policy maker has no credibility and the public expects that the discretionary inflation rate  $(\pi_{D,t})$  will be produced in the present period.
- The public adopt the "tit-for-tat" strategy in the repeated prisoner's dilemma game that it plays with the policy maker. If the policy maker "misbehaves" it gets punished by the public for one period.

## Reputation (2)

- Consider a policy maker in period 0 which kept its promise and produced the rule inflation in the period before [i.e. in period -1 it set  $\pi_{-1}=\pi_R$ ]. This policy maker has credibility in period 0 and the public expects  $\pi_0^e=\pi_R$ . The policy maker can do two things in period 0:
  - Keep its promise and maintain its reputation [produce  $\pi_0 = \pi_R$ ]. No punishment takes place!
  - Cheat in period 0 by producing  $\pi_C$  in that period [temptation is present because  $\Omega_R(\pi_R) > \Omega_C(\pi_R)$ ]. But because he broke his promise, the public punishes the policy maker and expect the discretionary solution next period  $[\pi_1^e = \pi_D]$ . This involves punishment because  $\Omega_D > \Omega_R(\pi_R)$  in period 1. In period 1 the public expects  $\pi_1^e = \pi_D$  and, given this expectation, it is optimal for the policy maker to produce  $\pi_D$ . So policy maker has reputation again in period 2 [as it kept its promise in period 1] and the public expects  $\pi_2^e = \pi_R$ .

## Reputation (3)

• The benefits of cheating [temptation] are:

$$T(\pi_R) \equiv \Omega_R(\pi_R) - \Omega_C(\pi_R)$$

$$= \frac{1}{2} \left[ \bar{y} - y^* \right]^2 + \frac{\beta}{2} \pi_R^2 - \frac{1}{2} \left[ \frac{\beta}{\alpha^2 + \beta} \left[ \bar{y} - y^* \right] - \frac{\alpha \beta}{\alpha^2 + \beta} \pi_R \right]^2$$

$$- \frac{\beta}{2} \left[ \frac{\alpha^2}{\alpha^2 + \beta} \pi_R + \frac{\alpha}{\alpha^2 + \beta} \left[ y^* - \bar{y} \right] \right]^2$$

• The costs of cheating [punishment] are:

$$P(\pi_R) \equiv \frac{\Omega_D - \Omega_R(\pi_R)}{1+r}$$

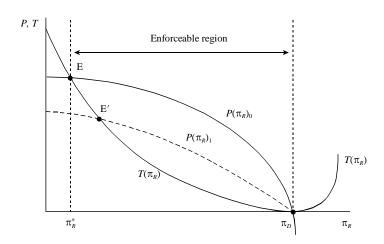
$$= \left[\frac{1}{2} \frac{\alpha^2 + \beta}{\beta} \left[\bar{y} - y^*\right]^2 - \frac{1}{2} \left[\bar{y} - y^*\right]^2 - \frac{\beta}{2} \pi_R^2\right] \frac{1}{1+r}$$

$$= \left[\frac{1}{2} \frac{\alpha^2}{\beta} \left[\bar{y} - y^*\right]^2 - \frac{\beta}{2} \pi_R^2\right] \frac{1}{1+r}$$

## Reputation (4)

- In Figure 9.2 we plot these two curves as a function of the rule inflation rate  $\pi_R$ .
  - Rule inflation rates between 0 and  $\pi_R^*$  and the ones exceeding  $\pi_D$  are such that the policy maker will always deviate from the rule. The temptation is too big.
  - Rule inflation rates between  $\pi_R^*$  and  $\pi_D$  are enforceable. The punishment exceeds the temptation and it is not worthwhile to deviate from the rule.
  - Since social welfare depends negatively on inflation, the optimal enforceable inflation rate is the lowest enforceable one, i.e.  $\pi_R^*$ .
  - If the interest rate rises,  $P(\pi_R)$  rotates counter-clockwise and the optimal enforceable inflation rate rises. Punishment more heavily discounted.

## Figure 9.2: Temptation and enforcement



## Voting and optimal inflation (1)

- Rogoff (1985) and Alesina & Grilli (1992) ask themselves why central bankers tend to be conservative economists.
- The median voter model of A & G can be used to cast some light on this issue. Which agent is elected to head the central bank?
- Person i has the following cost function:

$$\Omega_i \equiv \frac{1}{2} [y - y^*]^2 + \frac{\beta_i}{2} \pi^2$$
 (S4)

- Note that  $\beta_i$  appears in (S4). The higher is  $\beta_i$  the more "right wing" we call this person.
- The Lucas supply curve is still given by:

$$y = \bar{y} + \alpha \left[\pi - \pi^e\right] + \varepsilon, \quad \alpha > 0$$

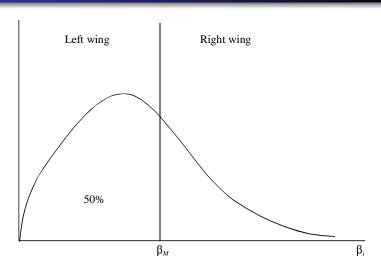
## Voting and optimal inflation (2)

 If person i would be the central banker then he/she would set inflation according to:

$$\begin{split} \pi_D^i &= \frac{\alpha}{\beta_i} \left[ y^* - \bar{y} \right] - \frac{\alpha}{\alpha^2 + \beta_i} \varepsilon \\ y_D^i &= \bar{y} + \frac{\beta_i}{\alpha^2 + \beta_i} \varepsilon \end{split}$$

• Assume that the distribution of  $\beta_i$  across the population is as in Figure 9.3. The person with preference parameter  $\beta_M$  is the *median voter* and effectively decides the election. [There is a single issue and preferences are single-peaked, so the median voter theorem holds].

# Figure 9.3: The frequency distribution of the inflation aversion parameter



## Voting and optimal inflation (3)

• The median voter's cost function is:

$$\begin{split} \Omega_M &\equiv \frac{1}{2} E \left( \left( y_D^i - y^* \right)^2 + \beta_M \left( \pi_D^i \right)^2 \right) \\ &= \frac{1}{2} E \left( \left( \underbrace{\bar{y} - y^* + \frac{\beta}{\alpha^2 + \beta} \varepsilon}_{(a)} \right)^2 + \underbrace{\beta_M}_{(b)} \left( \underbrace{\frac{\alpha}{\beta} \left( y^* - \bar{y} \right) - \frac{\alpha}{\alpha^2 + \beta} \varepsilon}_{(c)} \right)^2 \right) \\ &= \frac{1}{2} \left[ 1 + \beta_M \left( \frac{\alpha}{\beta} \right)^2 \right] (\bar{y} - y^*)^2 + \frac{1}{2} \frac{\beta^2 + \beta_M \alpha^2}{(\alpha^2 + \beta)^2} \sigma^2 \end{split}$$

- $\rightarrow$  Median voter cannot observe  $\varepsilon$  but he knows how banker of type  $\beta$  reacts to  $\varepsilon$ .
- (a) Output gap a central banker of type  $\beta$  would create.
- (b) Evaluated from the point of view of the median voter.
- (c) Inflation a central banker of type  $\beta$  would create.

## Voting and optimal inflation (4)

- The median voter elects central banker such that  $\Omega_M$  is minimized by choice of  $\beta$ .
- The first-order condition is:

$$\begin{split} \frac{d\Omega_M}{d\beta} &= -\frac{1}{2} 2\beta_M \frac{\alpha^2}{\beta^3} \left( \bar{y} - y^* \right)^2 \\ &+ \frac{1}{2} \frac{2(\alpha^2 + \beta)^2 \beta - 2(\beta^2 + \beta_M \alpha^2)(\alpha^2 + \beta)}{(\alpha^2 + \beta)^4} \sigma^2 = 0 \quad \Rightarrow \\ \frac{d\Omega_M}{d\beta} &= -\frac{\beta_M}{\beta} \left( \frac{\alpha}{\beta} \right)^2 (\bar{y} - y^*)^2 + \frac{(\beta - \beta_M)\alpha^2}{(\alpha^2 + \beta)^3} \sigma^2 = 0 \end{split}$$

• It follows that the optimal  $\beta$  exceeds  $\beta_M$ . The median voter delegates the conduct of monetary policy to someone more conservative than he is himself. This way the median voter commits to a lower inflation rate.

# Dynamic consistency and capital taxation (1)

- Dynamic inconsistency can also play a role in fiscal policy. We give the example of capital taxation.
- Two-period model (t = 1, 2)
- Household utility:

$$U \equiv \frac{C_1^{1-1/\varepsilon_1}}{1-1/\varepsilon_1} + \frac{1}{1+\rho} \left[ C_2 + \alpha \frac{(1-N_2)^{1-1/\varepsilon_2}}{1-1/\varepsilon_2} + \beta \frac{G_2^{1-1/\varepsilon_3}}{1-1/\varepsilon_3} \right]$$

## Dynamic consistency and capital taxation (2)

Technology:

$$F(N_t, K_t) = aN_t + bK_t$$

- Production factors perfect substitutes.
- Inessential production factors.
- Constant marginal products.
- Resource constraints:

$$C_1 + [K_2 - K_1] = bK_1$$
  
 $C_2 + G_2 = F(N_2, K_2) + K_2 = aN_2 + (1+b)K_2$ 

Note that these are expressions like "Y = C + I + G".

## First-best command optimum

• A benevolent social planner would choose  $C_1$ ,  $C_2$ ,  $N_2$ , and  $G_2$  such that household utility is maximized subject to the consolidated resource constraint:

$$C_1 + \frac{C_2 + G_2 - aN_2}{1+b} = (1+b)K_1$$

The solutions are:

$$C_1 = \left(\frac{1+b}{1+\rho}\right)^{-\varepsilon_1}$$
$$1 - N_2 = (a/\alpha)^{-\varepsilon_2}$$
$$G_2 = \beta^{-\varepsilon_3}$$

 The FBCO can be decentralized [i.e. reproduced in a free market setting] provided the policy maker has access to lump-sum taxes.

## Second-best optimum (1)

- What happens if lump-sum tax is not available and only distorting taxes can be used to obtain revenue [needed to pay for the public good]?
- The GBC becomes:

$$G_2 = t_K b K_2 + t_L a N_2$$

• The market solution becomes:

$$C_{1} = \left(\frac{1 + b(1 - t_{K})}{1 + \rho}\right)^{-\varepsilon_{1}}$$

$$C_{2} = a(1 - t_{L}) + (1 + b)\left[1 + b(1 - t_{K})\right]K_{1}$$

$$- (1 + \rho)^{\varepsilon_{1}}\left[1 + b(1 - t_{K})\right]^{1 - \varepsilon_{1}} - \alpha^{\varepsilon_{2}}\left[a(1 - t_{L})\right]^{1 - \varepsilon_{2}}$$

$$1 - N_{2} = \left(\frac{a(1 - t_{L})}{\alpha}\right)^{-\varepsilon_{2}}$$

## Second-best optimum (2)

- Non-zero  $t_K$  and/or  $t_L$  drive the market solution away from the FBCO. We cannot set  $t_L = t_K = 0$  because that would imply zero G [which is not optimal]. What do we do?
- We trade off the distortions in the tax system as well as we can by choosing G,  $t_L$ , and  $t_K$  such that welfare of the household is maximized given the absence of lump-sum taxes!
- The optimality conditions are the GBC plus:

$$\beta G_2^{-1/\varepsilon_3} = \eta \tag{S5}$$

$$\eta = \frac{1}{1 - \left(\frac{t_L}{1 - t_L}\right)\varepsilon_L} \tag{S6}$$

$$\eta = \frac{1}{1 - \left(\frac{t_K}{1 - t_K}\right)\varepsilon_K} \tag{S7}$$

# Second-best optimum (3)

- Continued.
  - $\eta$  is the marginal cost of public funds [MCPF].
  - ullet  $arepsilon_L$  is the uncompensated wage elasticity of labour supply.
  - ullet  $\varepsilon_K$  is the uncompensated interest elasticity of gross saving.
  - Equation (S5) is the "modified Samuelson rule".
- Equations (S6) and (S7) can be solved for the optimal tax rates:

$$\frac{t_L}{1 - t_L} = \left(1 - \frac{1}{\eta}\right) \frac{1}{\varepsilon_L} \tag{S8}$$

$$\frac{t_K}{1 - t_K} = \left(1 - \frac{1}{\eta}\right) \frac{1}{\varepsilon_K} \tag{S9}$$

The intuition is as follows: the objective is to tax in the least distorting fashion by taxing most heavily the most inelastic tax base (e.g. if  $\varepsilon_L=0$  then  $1/\varepsilon_L\to\infty$ ,  $\eta=1$ , and  $t_K=0$ . Labour income source of inelastic tax base in this special case).

## Second-best optimum (4)

- BUT!!! In the general case, with both taxes non-zero, taxing labour in period 2 is not efficient. Once period 2 comes along,  $K_2$  is inelastic and  $t_L=0$  and  $t_K>0$  is optimal. Hence, solutions in (S8) and (S9) are dynamically inconsistent.
- To find the consistent solution we would have to work backwards. we know that  $t_L=0$  and  $t_K>0$  in period 2. Then we can figure out what  $t_L$  and  $t_K$  should be in the first period.

#### **Punchlines**

- Dynamic inconsistency is all around us
- In the context of monetary policy a reputational mechanism can make a rule-based inflation rate enforceable.
- The median voter can commit to a lower inflation rate by electing a central banker who is more conservative than himself
- The optimal taxes on labour and capital suffer from the dynamic inconsistency problem.